# Separation of Carbon Dioxide by Asymmetric Hollow Fiber Membrane of Cellulose Triacetate

#### E. SADA, H. KUMAZAWA,\* J.-S. WANG, and M. KOIZUMI

Department of Chemical Engineering, Kyoto University, Kyoto 606-01, Japan

#### SYNOPSIS

Permeation behavior of pure  $CO_2$ ,  $O_2$ , and  $N_2$  and separation characteristics of  $CO_2$ -air mixtures were examined using hollow fiber modules of asymmetric cellulose triacetate membrane at 30°C. The ideal separation factor for  $CO_2$  relative to  $N_2$  ranged from 21 to 24. Permeation behavior for pure  $CO_2$  was interpreted in terms of the total immobilization model, i.e., a limiting case of the dual-mode mobility model for glassy polymer, where the diffusion coefficient for Henry's law mode is not assumed to be constant and depends on gas pressure via a modified free-volume model. Based on pure gas permeabilities to  $CO_2$ ,  $O_2$ , and  $N_2$ , simulation for the separation of  $CO_2$ -air mixtures was made using a countercurrent plug flow model, and the result fitted the corresponding experimental data fairly well. Membrane plasticization induced by  $CO_2$  had negligible effect on permeation to mixture of  $CO_2$  and air in the range of  $CO_2$  composition up to 50% and upstream total pressure up to 1.5 MPa.

## INTRODUCTION

Nowadays the global warming issue caused by greenhouse gases has become a matter of great concern, and carbon dioxide has widely been recognized as one of the most affecting greenhouse gases. Industry is one of the major sources of  $CO_2$ . Many plants such as fossile-fuel-fired power plants, iron and steel works, and cement works discharge a huge amount of  $CO_2$  day after day. Since  $CO_2$  emission will increase with energy consumption, intensive efforts must be made toward energy conservation and promotion of energy efficiency. Furthermore, the processes for removal, recovery, and fixation of  $CO_2$  emitted from stationary sources are of increasing importance.

The use of membrane technology for industrial gas separations has been shown to be practical and economical. Among many kinds of polymer membranes, cellulose triacetate membrane is known for its high permeability to  $CO_2$ . In the present work, we investigated the possibility of separating  $CO_2$  and air mixture with asymmetric hollow fiber membrane module of cellulose triacetate. This has been done by measuring permeation rates through the hollow fibers for pure  $CO_2$ ,  $O_2$ , and  $N_2$ , and carrying out separation experiments for  $CO_2$ -air mixtures. Permeabilities for the pure gases and separation factors for  $CO_2$  relative to  $N_2$  were calculated then. Simulation results for the mixtures based on a countercurrent plug flow model using permeation data of the pure gases were successfully compared with the experimental results. The plasticization effect of dissolved  $CO_2$  on permeation behavior of  $CO_2$ -air mixture was also considered.

## **EXPERIMENTAL**

Permeation and separation experiments were carried out using a membrane permeator of hollow fiber type. The details of the permeator were described elsewhere.<sup>1</sup> The unit consists of a bundle of asymmetric hollow fibers. An asymmetric hollow fiber of cellulose triacetate membrane has the skin layer on the outer surface, and the feed-outside operation mode was employed. That is, the feed gas is on the skin side of the asymmetric membrane.

Asymmetric hollow fiber modules of cellulose triacetate were provided by Toyobo Co. Ltd., Japan. Four modules with different dimensions have been used in the experiments. The module specification

<sup>\*</sup> To whom correspondence should be addressed. Journal of Applied Polymer Science, Vol. 45, 2181–2186 (1992) © 1992 John Wiley & Sons, Inc. CCC 0021-8995/92/122181-06\$04.00

 Table I
 Dimensions of Membrane Modules

Sample No.	11	12	13	31
$D_o$ (mm)	0.148	0.184	0.178	0.156
$D_i$ (mm)	0.056	0.091	0.087	0.063
$L_t$ (cm)	22	20	21	26
$N_t$	180	240	240	270
$A_t (\mathrm{cm}^2)$	184	278	282	338

is shown in Table I. Samples 11 and 31 are similar in outer and internal diameters of hollow fibers but are different in the total outer surface (permeation) area. Samples 12 and 13 are similar in the total outer surface area as well as the outer and internal diameters. The thickness of asymmetric membrane portion in all of four modules is nearly the same, ranging from 0.0455 to 0.0465 mm.

First, permeation experiments were conducted for pure CO<sub>2</sub>, O<sub>2</sub>, and N<sub>2</sub>. Then, mixtures of CO<sub>2</sub> and air containing 10, 20, and 50% CO<sub>2</sub> were permeated, and separation behavior was investigated. The composition of the permeates was determined by a gas chromatograph with a 2.5-m-long column packed with Porapak Q. The column temperature was held at 50°C, and helium was used as the carrier gas.

For the sake of comparison with permeation and separation behavior of asymmetric hollow-fiber-type membranes, experiments with the above-mentioned gases were also performed using flat homogeneous dense membranes of the same cellulose triacetate. The permeation cell is the same one as in our previous work.<sup>2</sup> The permeation area of the cell is 19.6  $cm^2$ . Cellulose triacetate samples were supplied by Fuji Film Co. Ltd., Japan. The nominal thickness of the film is 50  $\mu$ m (FT 0.05). The permeation rate for  $CO_2$  was calculated by flowing helium as a pickup gas at a prescribed rate on the downstream side and determining the concentration of CO<sub>2</sub> by means of the gas chromatograph. The flow rate of pickup gas was adjusted so that the partial pressure of  $CO_2$ might be regarded substantially as zero.

All of the experiments were carried out at 30°C and upstream total pressure up to 2.4 MPa for pure gases and 1.5 MPa for gas mixtures.

## EXPERIMENTAL RESULTS AND DISCUSSION

#### Permeation to Pure Gas

Measured steady-state permeation rate for pure gases were converted to the permeation rate coefficients defined by

$$\kappa = \frac{\bar{P}}{\delta} = \frac{J_s}{p_2 - p_1} \tag{1}$$

where  $\bar{P}$  refers to the mean permeability coefficient and  $\delta$  to the thickness of the skin layer of the asymmetric hollow fiber membrane. The permeation rate coefficients for N2, O2, and CO2 in asymmetric hollow fiber modules 11, 12, and 31 were plotted against the difference between pressures of feed and permeate sides in Figure 1. The coefficients for  $O_2$  and  $N_2$  are shown to be almost independent of the pressure difference, whereas those for  $CO_2$  increase with increasing pressure difference. For the four modules, values of the permeation rate coefficients for  $CO_2$ ,  $O_2$ , and  $N_2$  in the limit of  $\Delta p \rightarrow 0$ , and separation factors defined as the ratio  $(\bar{P}/\delta)_{\Delta p \rightarrow 0}$  for CO<sub>2</sub> to N<sub>2</sub> are listed in Table II. The separation factors for modules 11, 12, and 13 range from 21 to 24. The separation factor for sample 31 is determined to be 17. This may be because the morphology of the skin layer of sample 31 is different from those of the other modules.

In order to find out whether the above-mentioned pressure dependence is caused by membrane material (cellulose triacetate) or just by module geometry, mean permeability coefficients for these three gases through a flat homogeneous membrane



**Figure 1** Permeation rate coefficients as a function of pressure difference for  $CO_2$ ,  $O_2$ , and  $N_2$  in asymmetric hollow fibers of cellulose triacetate [sample no. 11 (half filled keys), no. 12 (open keys), no. 31 (filled keys)] at 30°C.

Table II Permeation Rate Coefficients<sup>a</sup> for  $CO_2$ ,  $O_2$ , and  $N_2$  and Separation Factors<sup>b</sup> for  $CO_2$ Relative to  $N_2$  in Hollow Fiber Membrane Modules at 30°C

	No. 11	No. 12	No. 13	No. 31
$(\bar{P}/\delta)_{ m CO_2}  imes 10^5$	4.5	4.0	6.2	6.1
$(\bar{P}/\delta)_{\Omega_2} \times 10^5$	1.0	0.90	1.5	1.8
$(\bar{P}/\delta)_{ m N_2}  imes 10^5$	0.20	0.17	0.29	0.39
α	22	24	21	17

<sup>a</sup> Values at the limit of  $\Delta p \rightarrow 0$ , [cm<sup>3</sup> (STP)/(cm<sup>2</sup> s cmHg)]. <sup>b</sup>  $\alpha = (\bar{P}/\delta)_{CO_2}/(\bar{P}/\delta)_{N_2}$ .

of cellulose triacetate were measured and plotted versus pressure difference, as shown in Figure 2. For  $N_2$  and  $O_2$ , the mean permeability coefficients are found to be essentially constant, and in the case of  $CO_2$  the coefficients increase with increasing pressure difference. This result conforms to the permeation results of the hollow fiber membrane module. In Table III, together with permeability coefficients for  $CO_2$ ,  $O_2$ , and  $N_2$  in the limit of  $\Delta p \rightarrow 0$ , the value of the ideal separation factor of the homogeneous membrane defined as the ratio of permeability for  $CO_2$  to that for  $N_2$  is listed.

The pressure dependence of  $\bar{P}/\delta$  and  $\bar{P}$  for CO<sub>2</sub> here seems to reflect plasticization effect induced by dissolved CO<sub>2</sub> and can be simulated in terms of the total immobilization model in conjunction with a modified free-volume model.<sup>3,4</sup> That is, the total im-



Figure 2 Permeability coefficients as a function of pressure difference for CO<sub>2</sub>, O<sub>2</sub>, and N<sub>2</sub> in a flat homogeneous membrane of cellulose triacetate at  $30^{\circ}$ C.

Table III	Permeability Coefficients <sup>*</sup> for $CO_2$ , $O_2$ ,
and N <sub>2</sub> and	l Separation Factors <sup>b</sup> for CO <sub>2</sub> Relative
to N <sub>2</sub> in a l	Flat Homogeneous Membrane at 30°C

$ar{P}_{ m CO_2}$	$6.4 imes10^{-10}$
$ar{P}_{ m O_2}$	$6.8 imes10^{-11}$
$ ilde{P}_{ m N_2}$	$2.0 imes10^{-11}$
α	32

<sup>a</sup> Values at the limit of  $\Delta p \rightarrow 0$ , [cm<sup>3</sup> (STP) cm/(cm<sup>2</sup> s cmHg)]. <sup>b</sup>  $\alpha = \vec{P}_{CO_2}/\vec{P}_{N_2}$ .

mobilization model, one limiting case of the dualmode mobility model is operative, where the diffusion coefficient for Henry's law mode is not assumed to be constant but depends on the gas pressure in terms of the modified free-volume model. According to such a model, the pressure dependence of the permeability coefficient should be linear or quadratic,<sup>5</sup> and therefore conforms to the experimental results for CO<sub>2</sub> depicted in Figures 1 and 2.

## Permeation for CO<sub>2</sub>-Air Mixtures

Typical separation results for the  $CO_2$ -air mixture containing 10 vol %  $CO_2$  are indicated in Figure 3 as a plot of concentration of  $CO_2$  in permeate stream  $(y_P)$  versus stage cut (defined as the fraction of the feed that has permeated). Permeability measurements were carried out at three feed pressure levels with constant permeate pressure (1 atm).

As shown in this figure, permeate with higher CO<sub>2</sub>



Figure 3 Relationship between mole fraction of  $CO_2$  in the permeate stream and stage cut at different upstream total pressures for a mole fraction of  $CO_2$  of 0.1 in upstream (sample no. 12).



**Figure 4** Relationship between mole fraction of  $CO_2$  in the permeate stream and stage cut at different upstream total pressures for a mole fraction of  $CO_2$  of 0.2 in upstream (sample no. 12).

concentration could be obtained at the same stage cut as the feed pressure was raised from 5.8 to 10.7 atm. Although the degree of this increase diminished as the feed pressure was raised further to 15.5 atm, higher permeation flux with unchanged separation factor was achieved. This is understandable if the permeabilities for penetrants remain the same as in their pure-gas cases, and no plasticization due to  $CO_2$  takes place (this will be discussed later).

The solid curves are simulation results using a simple countercurrent plug flow model,<sup>6</sup> where the high- and low-pressure gas streams flow countercurrently to one another, and the total pressure is uniform in both the streams. A  $CO_2$ -air mixture is treated as a ternary system of  $CO_2$ ,  $O_2$ , and  $N_2$ , and their pure-gas permeabilities are used in the calculation. The lower, middle and upper solid curves represent simulation results, respectively, for the feed pressures of 5.8, 10.7, and 15.5 atm.

Simulation results for  $CO_2$ -air mixtures containing 20 and 50%  $CO_2$  are shown as solid curves in Figures 4 through 6 in comparison with experimental points. Similarly, the solid curves from the bottom upward represent simulation results for the feed pressures in order. It can be seen that, except in low stage cut region where some deviation appears, the agreement between simulation results and experimental data is satisfactory.

The separation experiments were carried out from low to high pressure through the three pressure levels. After the highest pressure, 15.5 atm, measurements were repeated at a low-pressure level to see



**Figure 5** Relationship between mole fraction of  $CO_2$  in the permeate stream and stage cut at different upstream total pressures for a mole fraction of  $CO_2$  of 0.5 in upstream (sample no. 13).

whether some change would occur or not. The point is that if under high partial pressure of  $CO_2$  the membrane might be plasticized, then the permeabilities for  $O_2$  and  $N_2$  would increase.<sup>7</sup> In this case it follows that the separation factor or  $y_P$  might decrease.<sup>8,9</sup> As indicated in Figures 5 and 6 by filled circles representing the data obtained from such repetition, even in the case of 50%  $CO_2$  mixture where  $CO_2$  partial pressure is up to about 8 atm, no change was detected.



**Figure 6** Relationship between mole fraction of  $CO_2$  in the permeate stream and stage cut at different upstream total pressures for a mole fraction of  $CO_2$  of 0.5 in upstream (sample no. 31).



**Figure 7** Dependence of permeability coefficient for  $CO_2$  in a flat homogeneous membrane of cellulose triacetate on partial pressure of  $CO_2$  in upstream at 30°C.

Since plasticization effect on cellulose triacetate membrane by  $CO_2$  has been reported by several authors, <sup>3,4,8,9</sup> to make sure that the above result is valid, permeability measurements with homogeneous cellulose triacetate membrane for  $CO_2$  and  $CO_2$ -air mixtures were conducted. The results are shown in Figure 7. It is obvious that pressure dependence of the permeability coefficient for  $CO_2$  in the mixture becomes weaker than that for pure  $CO_2$  at the same partial pressure of  $CO_2$ . This could be attributed to a competition among the penetrants for unrelaxed volume in the membrane.<sup>8,10</sup> Due to this effect, the solubility of  $CO_2$  is reduced. The decrease in solubility can in turn reduce diffusivity. As a result, the permeability for  $CO_2$  is lowered by the presence of air. Especially in the region below 8 atm (the pressure corresponding to the highest partial pressure of  $CO_2$  in the separation experiments), the permeability coefficients practically do not change with increasing pressure. Therefore, it can be expected that in the separation experiments of this work, the change in permeability for  $CO_2$  due to the plasticization effect can be neglected.

The deviations of the simulation curves from experimental data at low stage cuts appear to be larger than experimental errors and could be due to the fact that the assumption of negligible pressure loss in the bore side is not satisfied, as high permeate flux induces pressure buildup inside the bore.

Nevertheless, the good agreement between the calculated values and experimental data suggests that in the range of the present work, permeation data of the pure gases can be used to predict the separation performance of the cellulose triacetate hollow fiber membrane module, and separation factors close to calculated ones could be achieved.

# **CONCLUSION**

The ideal separation factor of asymmetric hollow fiber membrane of cellulose triacetate for  $CO_2$  relative to N<sub>2</sub> at 30°C ranged from 21 to 24. Permeation behavior for pure  $CO_2$  was interpreted in terms of the total immobilization model, where the diffusion coefficient for Henry's law mode depends on gas pressure via a modified free-volume model, whereas that for pure  $O_2$  and  $N_2$  could be interpreted in terms of a simple solution diffusion model. Based on pure gas permeabilities to  $CO_2$ ,  $O_2$ , and  $N_2$ , simulation for the separation of CO<sub>2</sub>-air mixtures was conducted using a countercurrent plug flow model, and the result fitted the experimental data fairly well. Membrane plasticization induced by  $CO_2$  has negligible effect on permeation to mixture of  $CO_2$  and air in the range of  $CO_2$  composition up to 50% and upstream total pressure up to 1.5 MPa.

## NOMENCLATURE

- $A_t$  total membrane area in the moule, cm<sup>2</sup>
- $D_i$  hollow fiber inside diameter, mm
- $D_0$  hollow fiber outside diameter, mm
- $J_s$  steady-state permeation flux, cm<sup>3</sup> (STP)/ (cm<sup>2</sup> s)
- $L_t$  total length of hollow fiber, cm
- p pressure, atm
- $p_1$  permeate outlet pressure or downstream pressure, atm

- $p_2$  feed-side pressure or upstream pressure, atm
- $y_P$  permeate concentration of  $CO_2$  in mole fraction
- $\alpha$  ideal separation factor of CO<sub>2</sub> relative to N<sub>2</sub>
- $\delta$  effective thickness of skin layer of asymmetric membrane, cm

 $\Delta p = p_2 - p_1$ , atm

- $\theta$  stage cut defined as the ratio of permeate flow rate to feed flow rate
- $\kappa = \bar{P}/\delta$ , permeation rate coefficient, cm<sup>3</sup> (STP)/(cm<sup>2</sup> s atm) or cm<sup>3</sup> (STP)/(cm<sup>2</sup> s cmHg)

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